

Theoretical Analysis of the Influence of the Refractive Index on Electromagnetic Wave Propagating through Manganese Sulphide [MnS]

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Abstract

The theoretical analysis of the Electromagnetic wave propagation through chemically bath deposited manganese sulphide thin film and optical properties were studied using beam propagation technique in which a scalar wave is propagated through the material thin film deposited on a substrate with the assumption that the refractive index of the medium has homogenous reference refractive index reference term, n_{ref} and a perturbed refractive index term, representing the deposited thin film medium is presented in this work. These are substituted into a defined scalar wave equation in which the appropriate Green's Function was defined on it and solved using series solution technique in conjunction with Born approximation method in order to obtain a model equation of wave propagating through the thin film. This was transformed to Volterra equation and used in computing the propagated field for different input regions of the field wavelength such as ultraviolet, visible and infrared region respectively during which the influence of the influence of the refractive index on the propagating wave through the thin film was considered. The results obtained from the computed field were used in turn to compute the band gaps and optical properties of the thin film.

Keywords: Wave Propagation; Manganese Sulphide Thin Film; and Chemical Bath Deposition; Refractive Index; Perturbation; Green's Function; Band Gap; Optical Properties

Introduction

Manganese (II) sulfide (MnS) is a p-type semiconductor with a direct and wide band gap ($E_g = \sim 2.05\text{eV}$ to 2.95 eV) [1] with the absorbance and reflectance having unique behavior within 0-400nm

wavelength [2-4] and undergoes a transition to an antiferromagnetically (AFM) ordered phase below room temperature [5]. These features attracted interest for the potential applications of nanosized MnS in the field of short wavelength optoelectronics [6-8] or as a photoluminescent component [9], photo reduction

catalysts [10], and contrast agent for magnetic resonance imaging (MRI) [11,12]. The optical properties of MnS have also raised considerable interest in photobiology since it is deemed to have played a key role (along with ZnS in mixed haloes formed around primeval sub-aerial hot springs) in the prebiotic photosynthesis development. More recently, interesting energy-related applications have been demonstrated, where MnS was employed as an electrode material in Li-ion batteries [13-15] and as a supercapacitor material [16,17]. These interesting properties and promising applications have raised considerable attention and research on small MnS particles that has been known to exist in three phases.

Three polymorphs (α , β , and γ) of MnS are known, and their crystal structure is distinct and can easily be differentiated. In the cubic rock-salt α -MnS structure, sulfide anions an expanded fcc lattice, and the manganese cations occupy all octahedral sites. The metastable form β -MnS has the cubic zincblende structure. Similarly to α -MnS, β -MnS comprises an expanded fcc lattice of S²⁻anions, but in this polymorph, the Mn²⁺ cations reside on half of the tetrahedral sites. Structurally, the cubic α -phase is stable at room temperature and also reasonably stable at all temperature [18,19]. Finally-MnS and γ -MnS has the hexagonal wurtzite structure, based on a slightly compressed ($c/a = 1.618$) hcp lattice of sulfide anions with manganese cations occupying half of the tetrahedral sites can be grown at low temperature but they easily transform to the more stable α -phase above 200°C. The polymorphs have similar but unequal physical properties; for instance, all the three forms of MnS undergo transition to an AFM ordered structure [20], but the transition temperature varies from TN \sim 80 K for γ -MnS to \sim 100 K for β -MnS and 154 K for α -MnS [8].

Many techniques have been used to grow the thin film such as Chemical Bath, [21,22] Although the process of growth and growth mechanism is not our main focus in this work but rather the mechanism involved in the process of characterization of the film in order to determine the applicability of the film which centers more on the way electromagnetic wave behaves as it propagates through the material we still need to high light the chemical bath growth technique which was the method used to grow the thin film we analyzed. This forms the inclination that brought about the use of wave propagation since the response by the material medium to the wave propagating through it is the determinant. Our method here involves propagating an input field over a small distance through the thin film medium and then iterating the computation over and over through the

propagation distance using Lippmann-Schwinger equation and its counterpart, Dyson's equation [23].

Various tools have been employed in studying and computing beam or field propagation in a medium with variation of small refractive index [24,25] some researchers had employed beam propagation method based on diagonalization of the Hermetician operator that generates the solution of the Helmholtz equation in media with real refractive indices [26] while some had used 2x2 propagation matrix formalism for finding the obliquely propagated electromagnetic fields in layered inhomogeneous un-axial structure [27]. Structure such as optical fibres, optical wave guides in the presence of electro-optical perturbation [28,29]. However, earlier before the, work had been going on veraciously on study of wave propagation in a stratified media, plasma and ionosphere [30]. Van Roey in his work derived a general beampropagation relation in a number of specific cases along with the extensive simulation of wave propagation in variety of material medium. The effect of variation of refractive index of FeS₂, influence of dielectric function and conductivity of thin film material on propagating wave through its medium had also been carried out [24,31,32]. A close look on the concept made it clear to recognize the importance of the effect of the refractive index of the medium in the reality of the two velocity components that normally give rise to phase and group refractive indices as considered study of wave propagation [33,34]. More complicated work are being embarked upon on the study of wave propagation through a modeled thin with dielectric perturbation in which W.K.B approximation in conjunction with numerical approach were used .In this work, we make use of theoretical concept to study the influence of refractive index on wave propagating through Manganese Sulphide thin film medium and use the approach to analyze the optical properties of the thin film circumventing the use of experiment that always involve a huge sum of fund for its growth and analysis coupled with lack of needed and required equipment for such work since research in nanoscience is the order of the day due to its technological applications.

In this our method here we involves the concept of propagation of an input field over a small distance through the thin film medium and then iterating the computation over and over through the propagation distance using Lippmann-Schwinger equation and its counterpart, Dyson's equation. In this case, we first derived Lippmann-Schwinger equation using a specific Hamiltonian from where the field function $\psi_k(z)$ was

obtained using a specific Hamiltonian from where the field function $\psi_k(z)$ and write it as Volterra equation from where the solution for Green's value is sought using the boundary condition $G(z, 0) = G(z, z')$ with which absorption characteristics is sought within the wavelength ultraviolet, visible and infra-red regions of electromagnetic wave spectrum aimed at analyzing the influence of the refractive index of the material thin film on the propagated wave from the theoretical solution.

Experimental Procedure of Growing Thin Films

Experimentally, glass slides are used as substrate in growing the films though they were first of all washed using soap solution and subsequently kept in hot chromic acid and then cleaned with deionized water followed by rinsing in acetone. Finally, the substrates were ultrasonically cleaned with deionized water for 10 min and wiped with acetone and stored in a hot oven at 40°C. Typically, 20ml of 1M manganese acetate tetrahydrate ($C_4H_6MnO_4 \cdot 4H_2O$) and 4 ml of 7.4 M triethanolamine ($C_6H_{15}NO_3$) (TEA) were vigorously mixed in 100 ml glass beaker for 5 min. After that, 20 ml of 1.5 M ammonia solution (NH_4OH) was added to the solution and further stirred for 10 min. Then under constant stirring, 0.4ml of hydrazine hydrate ($H_4N_2H_2O$) (80%) solution was mixed followed by 20 ml of 1.4 M thioacetamide (C_2H_5NS) and the solution was stirred for 10 min. The final solution was made 75 ml by adding double distilled water. The pH of the bath solution was found to be 11. The already cleaned micro-scope glass slides were used as substrates. The glass slide substrate was immersed in the prepared bath solution and kept vertical in the beaker for thin film deposition. The deposition was done at room temperature. After 6 h, the glass slide was removed, rinsed with double distilled water and allowed air drying. Many trials were conducted to optimize the deposition parameters to obtain a good quality MnS thin film. The resultant films were homogeneous and well adhered to the substrate with mirror like surface. The deposited glass beaker for 5 min. After that, 20 ml of 1.5 M ammonia solution (NH_4OH) was added to the solution and further stirred for 10 min. Then under constant stirring, 0.4ml of hydrazine hydrate ($H_4N_2H_2O$) (80%) solution was mixed followed by 20 ml of 1.4 M thioacetamide (C_2H_5NS) and the solution was stirred for 10 min. The final solution was made 75 ml by adding double distilled water. The pH of the bath solution was found to be 11. The already cleaned micro-scope glass slides were used as substrates. The glass slide substrate was immersed in the prepared bath

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Theoretical and Analytical Frame Work

In this concept, we start by considering scalar wave equation as given below that defines general expression for wave propagating through an arbitrary medium.

$$\nabla^2 \psi(r) + \omega^2 \epsilon_o \mu_o \psi(r) = 0 \quad (1) a$$

But however, in this equation we introduce a perturbation that defines refractive index in thin film medium and reference refractive index n_{ref} representing a space without thin film and a refractive index in the thin film medium $Dn_p(z)$ where the thin film is as shown the Figure 1 below.

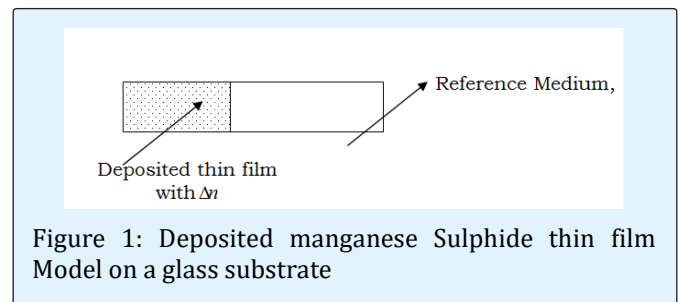


Figure 1: Deposited manganese Sulphide thin film Model on a glass substrate

where the Refractive index function as defined in equation (1)

$$n_p = n_{ref} + \Delta n(z) \quad (1) b$$

The wave equation relating our model can be written as

$$\nabla^2 \psi(z) = -k^2 n_{ref}^2 \psi(z) - k^2 \Delta n \psi(z) \quad (2)$$

For us to get a meaningful solution to the problem, second term on the right side would be considered to be zero, such that

$$\nabla^2 \psi(z) + k^2 n^2 \psi(z) = 0 \quad (3)$$

If the field value for $z = z_0$ is known for radiation at infinity, the propagating field, ψ and its gradient $\frac{\partial \psi}{\partial z}$

can be determined for all the values of the propagating distant, z by means of an operator A^\dagger which now transforms our expression as

$$\frac{\partial \psi_1}{\partial z} = A^\dagger \psi(z) \text{ and } \frac{\partial \psi_2}{\partial z} = B^\dagger \psi(z) \quad (4)$$

Where the operator, A^\dagger and B^\dagger signify the transverse coordinate of the field in first and second terms in (4).

The Green's function for our problem can be deduced by first of all constructing the Green's function which involves the solutions of the homogeneous equation (3) that will enable us write the Dyson's equation as thus

$$\psi(z, z') = \int_0^{z'} G(z, z') V(z') \psi(z') dz' \quad (5)$$

Given $G(z, z')$ the Green's function specified by;

$$G(z, z') = \frac{2}{z} \sum_{n=1}^{\infty} \frac{\sin(n\pi z'/z)}{\gamma^2 - \frac{n^2 \pi^2}{z^2}} \quad (6)$$

$$V(z) = -\gamma^2 \Delta n_p(z) = -\gamma^2 (n_p(z) - n_{ref}) \quad (7)$$

Linearizing $n(z)$ as follows;

$$n(z) \approx n_0 + kz + o(z^2), \quad (8)$$

We neglect higher order terms as we are dealing with thin film,

Where ϵ_0 and k are constants,

$$\begin{aligned} V(z) &= -\gamma^2 \Delta n(z) = -\gamma^2 (n(z) - n_{ref}) \\ &= -\gamma^2 (n_0 - n_{ref} + kz) \\ &= -\gamma^2 (n' + kz) \end{aligned} \quad (9)$$

Furthermore, we have $\psi(z') = \sin\left(\frac{2\pi}{\lambda} z'\right)$

Hence the integral becomes;

$$\psi(z) = \int_0^{z'} \frac{2}{z} \sum_{n=1}^{\infty} \frac{\sin(n\pi z'/z)}{\gamma^2 - \frac{n^2 \pi^2}{z^2}} (-\gamma^2 (n' + kz')) \sin\left(\frac{2\pi}{\lambda} z'\right) dz' \quad (10)$$

Hence we replaced ϵ' by ϵ and write

$$I(z, z') = -\gamma^2 \int_0^{z'} \frac{2}{z} \sum_{n=1}^{\infty} \frac{\sin(n\pi z'/z)}{\gamma^2 - \frac{n^2 \pi^2}{z^2}} (n + kz') \sin\left(\frac{2\pi}{\lambda} z'\right) dz' \quad (11)$$

In which we obtain the integral as

$$\psi(z, z') = -\frac{2}{z} \sum_{n=1}^{\infty} \frac{\gamma^2}{\left(\gamma^2 - \frac{n^2 \pi^2}{z^2}\right)} \int_0^{z'} \sin(m\pi z'/z) (n+kz') \sin\left(\frac{2\pi}{\lambda} z'\right) dz' \quad (12)$$

$$G(z, z')$$

$$= -\frac{2}{z} \sum_{n=1}^{\infty} \frac{\gamma^2}{\left(\gamma^2 - \frac{m^2 \pi^2}{z^2}\right)} \times$$

$$\left[\begin{aligned} & \frac{n\pi \backslash m^3 \lambda^3 \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 2\varepsilon\pi m^2 \lambda^2 z \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 4\varepsilon\pi n \lambda z^2 \sin\left[\frac{(2z+n\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \\ & + \frac{2n\pi m^2 \lambda^2 z \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] - 4k\pi m \lambda z^2 \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] - 8m\pi z^3 \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \\ & + \frac{8k\pi z^3 z' \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 8k\pi z^3 z' \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] - 4km\lambda^2 z^2 \cos\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \\ & + \frac{-4n\pi m \lambda z^2 \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] + km^2 \lambda^3 z \cos\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] + n\pi m^3 \lambda^3 \sin\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \\ & + \frac{k\pi m^3 \lambda^3 z' \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] + 4kz^3 \lambda \cos\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 2k\pi m^2 \lambda^2 z' z \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - n^2 \lambda^2)^2} \\ & + \frac{-kn^2 \lambda^3 z \cos\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] + 8\varepsilon\pi z^3 \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 4kz^2 \lambda^2 n \cos\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right]}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \\ & + \frac{-4kz^3 \lambda \cos\left[\frac{(2z-m\lambda)\pi z'}{\lambda z}\right] - 4k\pi z^2 \lambda m z' \sin\left[\frac{(2z+m\lambda)\pi z'}{\lambda z}\right] - 4km\lambda^3 z^3}{\pi^2 (4z^2 - m^2 \lambda^2)^2} \end{aligned} \right] \quad (13)$$

Analytically, the Green's function could be obtained by using Green's function series expansion solution technique with boundary condition that

$$G(z, 0) = G(z, z') \quad (14)$$

As the right hand vanishes at the end of the interval (0,z) which makes possible to expand the function in a suitably chosen orthogonal functions such as Fourier series [24].

The solution of the inhomogeneous part of the film becomes

$$\psi(z, z') = \int_0^z G(z, z') f(z') dz' \quad (15)$$

Where $f(z') = k \Delta n^2 \psi(z')$ (16)

The series solution of the problem becomes

$$G(z, z') = \frac{2z}{\pi^2} \sum_{m=1}^{\infty} \frac{1}{m} \sin\left(\frac{m\pi z'}{z}\right) \int_0^a f(z') \sin\left(\frac{m\pi z'}{z}\right) dz' \quad (16)$$

Assuming Δn to be periodic, we can write

$$\rho_m = \int_0^a f(z') \sin\left(\frac{m\pi z'}{z}\right) dz' \quad (17)$$

$$\psi(z, z') = \frac{2z}{\pi^2} \sum_{m=1}^{\infty} \frac{1}{m^2} \rho_m \sin\left(\frac{m\pi z'}{z}\right) \quad (18)$$

Analysis of the Influence of Refractive Index on the Propagating Wave

Considering the wave to be propagating through the film towards the increasing z with no paraxiality, we split the increasing wave into two parts with ψ_1 being regarded as the wave propagating from higher refractive index region of the thin film and ψ_2 as the part propagating through the less refractive index region respectively. The total sum of the propagating wave in the medium becomes

$$\psi = \psi_1 + \psi_2 \quad (19)$$

This could be written as

$$\frac{\partial \psi}{\partial z} = A^\dagger \psi_1 + B^\dagger \psi_2 \quad (20)$$

Analytically, equation (20) is an important approximation, though it appears to restrict the use of beam propagation technique in the study of the influence of the reflected wave on the forward propagating one in a structured thin film material except where there is a variation in the refractive index as a function of the propagating distance in which case the reflected wave adds up coherently to the propagating wave and since the Green's function as obtained in our formalism satisfies

$$\left[\left(\frac{\partial^2}{\partial z^2} + \frac{\partial^2}{\partial z'^2} \right) \Delta n(z, z') \right] G(z, z') = \delta(z - z') \delta(z' - z), \quad (21)$$

at the boundary source point in conjunction with the impedance boundary condition

$$G(z, z') + \beta_o \frac{\partial G(z, z')}{\partial n} \quad (22)$$

where $\beta_o = \frac{iR_s}{kR_o}$ and $R_o = \left[\frac{\mu_o}{\epsilon_o} \right]^{1/2}$

and R_s and R_o signifies the characteristic impedance offered by the thin film medium to the propagating wave and that of the free space impedance respectively which is given by

$$R_s = \frac{R_o}{n} \left[1 - \frac{1}{n^2} \right] \quad (23)$$

For every given wave of wavelength, λ propagating through the thin film medium of refractive index, n, the impedance is expressed as in equation (23). With the knowledge of the impedance, the absorption coefficient of the propagating wave is computed and in turn used for further application.

This is the situation that enabled us to consider it valid in the computation of the absorption coefficient that was applied in computation of the band gap, and other optical properties of the thin film.

In all use we considered in analysis the wavelength within $\lambda = 250\text{nm}$ to 1200nm

From the equation, it is obvious that ($\psi(z)$ tends to 0 as the dielectric constant $\epsilon' \rightarrow \infty$,

Therefore for fixed values of other parameters, the resultant solution can be approximated to any number of terms as may be required in relation to wave propagation terms

This is used to obtain the absorption co-efficient using

$$I = I_0 \exp \alpha z$$

$$\alpha = \frac{1}{z} \ln \left(\frac{I}{I_0} \right) \quad (24)$$

known as Lamber-Beer- Bouguer law and the transmittance is obtained from

$$T = \frac{(1-R)^2 \exp -\alpha t}{1-R^2 \exp -2\alpha t} \quad (25)$$

The reflectance is also deduced in terms of absorption coefficient as

$$R = \frac{1 \pm (1 - \exp(-\alpha t)) + \exp \alpha t}{1 + \exp(-\alpha t)} \quad (26)$$

While from the values of the reflectance the refractive index of the film which is wavelength dependent can be obtained from the equation

$$n = \frac{(R+1) + (3R^2 + 10R - 3)}{2(R-1)} \quad (27) \quad [20]$$

The absorption coefficient is used in equation (25) to plot the graph from where the band gap of the film should be deduced

$$(\alpha h\nu)^2 = A [h\nu - E_g] \quad [40] \quad (28)$$

Result/Discussion

The computed field ψ as a function of Green' values, G were presented in Figures 2-4 where it is seen that the optimum value of the field was located at the point where the Green's value is 0.45 in all the graphs for the UV, Visible and Infra-red region of electromagnetic wave. This made it more paramount for us to use a constant value of the green's value in subsequent computation of other parameters where G was needed especially in analyzing the wave profiles as it propagates through the thin film medium as shown in Figures 5-7 in which it is clearly seen that UV exhibited a negative value of the field profile while visible and infrared appeared on the positive value of the field. Specifically, the wave profiles varies with the propagation distant where it is seen that visible and infrared have the highest field within $0.1\mu\text{m}$ with a decrease on the value of the field as the propagation distant increased to $0.50\mu\text{m}$. On the other hands, UV experienced a minimum value within $0.10\mu\text{m}$ experiencing the highest field value at $4.50\mu\text{m}$ of the propagation distant. The of the behavior profiles in this manner probably seems to be reflected on the optical

response of the thin film to electromagnetic wave propagation through it. The absorbance and transmittance are as shown in Figures 8-10 where was observed that the absorbance profile for the film in UV and blue regions appears negative; the reflectance is negative all through within all the regions as shown in Figure 11. The transmittance exhibited selective behavior within some windows as seen in Figure 10 and 11. The band gap values were obtained from extrapolated graphs of equation (20) which were plotted according to wavelengths within the three regions considered in this work which implies that the band gap was marched to a particular wavelength as shown in Figure 12.

(a) $\lambda=250\text{nm}$ 2.77eV (c) $\lambda=750\text{nm}$ 2.24eV (e) $\lambda=1200\text{nm}$ 2.08eV
(b) $\lambda=500\text{nm}$ 2.33eV (d) $\lambda=1000\text{nm}$ 2.19eV

The average of the band gap for all the wavelength is 2.68eV

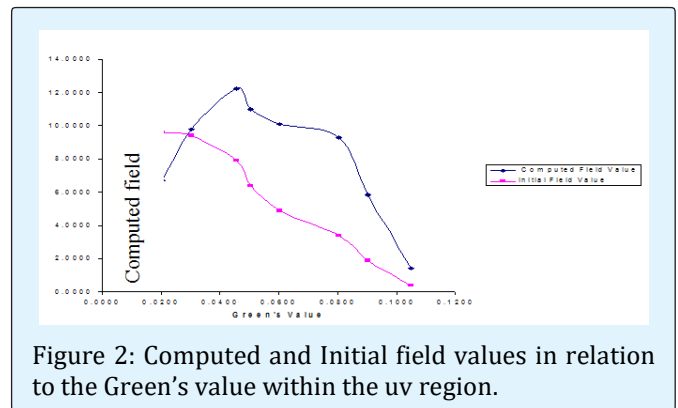


Figure 2: Computed and Initial field values in relation to the Green's value within the uv region.

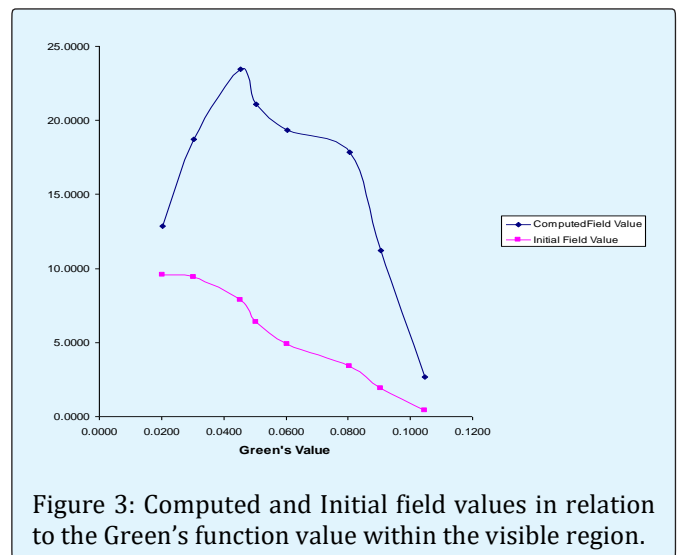


Figure 3: Computed and Initial field values in relation to the Green's function value within the visible region.

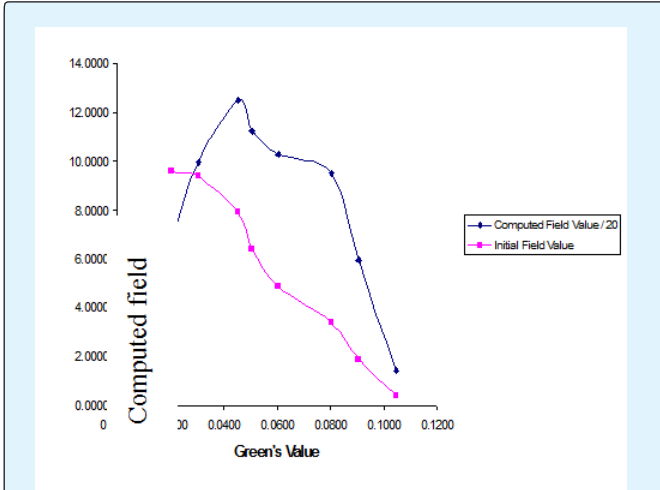


Figure 4: Computed and Initial field values in relation to the Green's function value within the near infrared region.

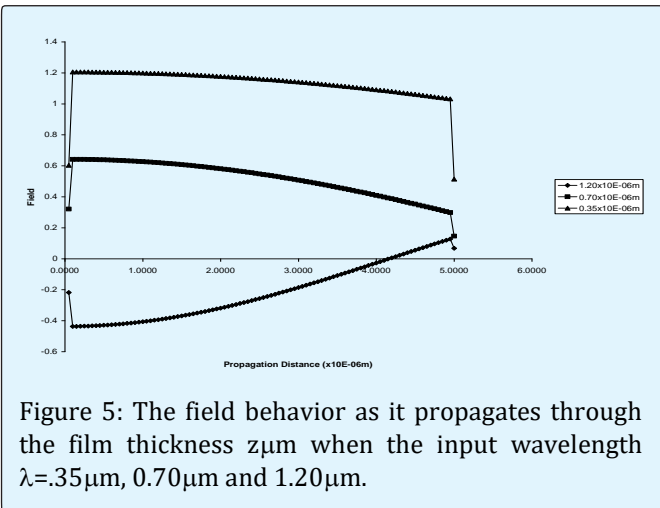


Figure 5: The field behavior as it propagates through the film thickness $z\mu\text{m}$ when the input wavelength $\lambda = .35\mu\text{m}$, $0.70\mu\text{m}$ and $1.20\mu\text{m}$.

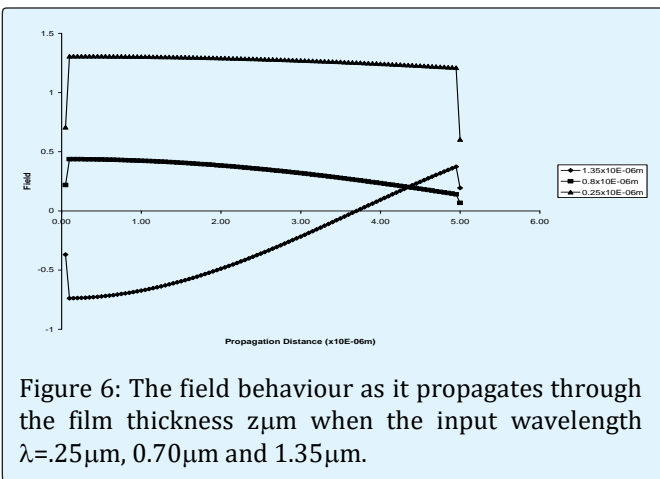


Figure 6: The field behaviour as it propagates through the film thickness $z\mu\text{m}$ when the input wavelength $\lambda = .25\mu\text{m}$, $0.70\mu\text{m}$ and $1.35\mu\text{m}$.

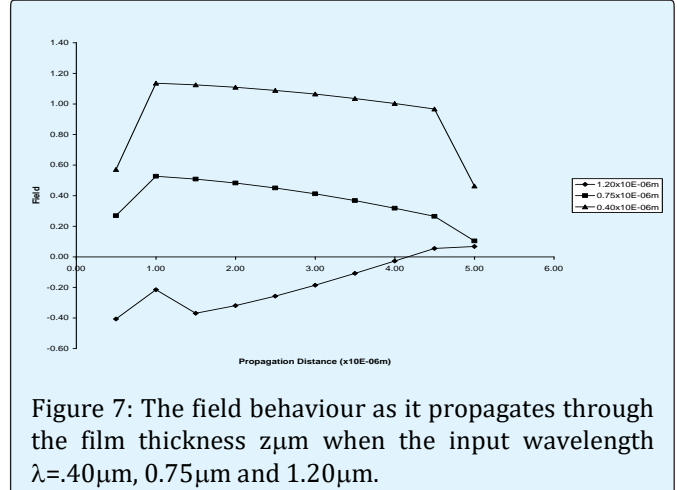


Figure 7: The field behaviour as it propagates through the film thickness $z\mu\text{m}$ when the input wavelength $\lambda = .40\mu\text{m}$, $0.75\mu\text{m}$ and $1.20\mu\text{m}$.

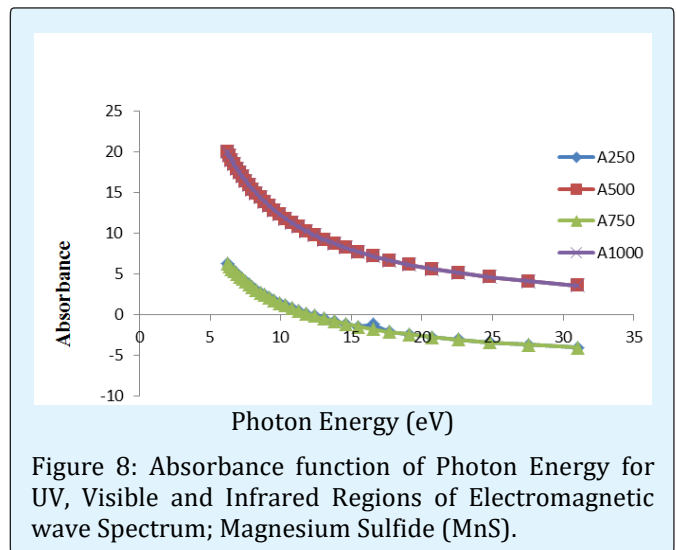


Figure 8: Absorbance function of Photon Energy for UV, Visible and Infrared Regions of Electromagnetic wave Spectrum; Magnesium Sulfide (MnS).

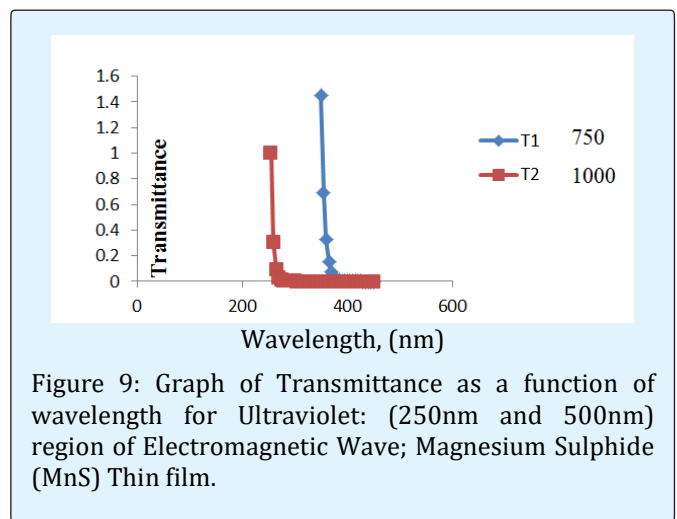


Figure 9: Graph of Transmittance as a function of wavelength for Ultraviolet: (250nm and 500nm) region of Electromagnetic Wave; Magnesium Sulphide (MnS) Thin film.

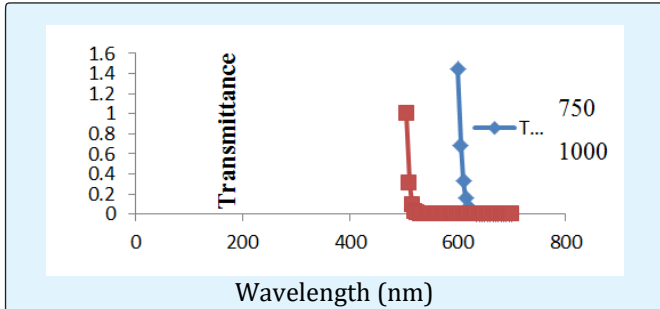


Figure 10: Graph of Transmittance as a function of wavelength for Visible (750nm and Infrared (1000nm) regions of Electromagnetic Wave; Magnesium Sulphide (MnS) Thin Film.

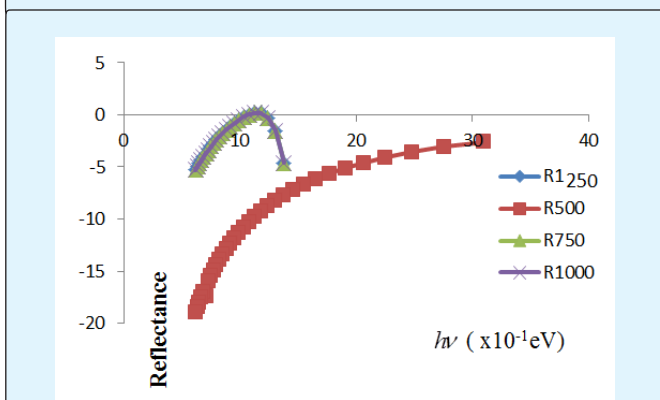


Figure 11: Reflectance as a function of Photon Energy for UV, Visible and Infrared Regions of Electromagnetic wave Spectrum; Magnesium Sulfide, (MnS) Thin Film.

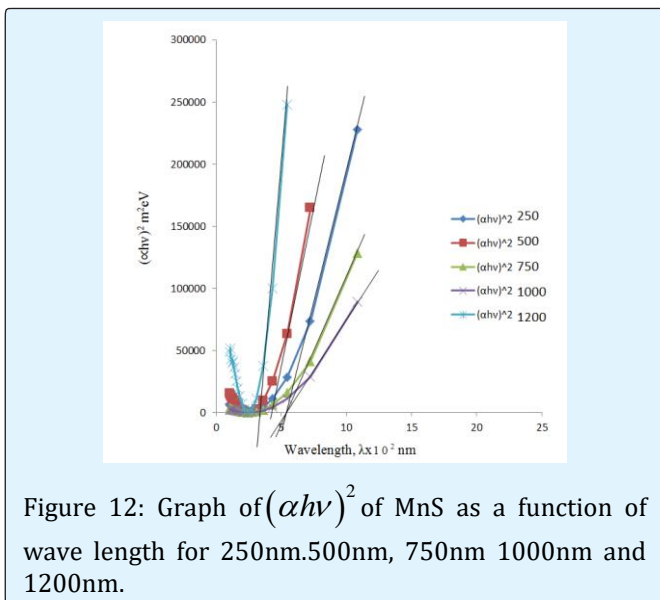


Figure 12: Graph of $(\alpha h\nu)^2$ of MnS as a function of wave length for 250nm, 500nm, 750nm, 1000nm and 1200nm.

Conclusion

Here theoretical and analytical studies have been carried out on the influence of the refractive index on the electromagnetic wave propagation through MnS thin film with refractive index n , where Green's function and Lippmann-Schwinger equations played prominent role in the mathematical formalism in conjunction with Volterra equation. The computed Green's values were used to analyze the behaviour of the wave profile and subsequently utilized in obtaining the absorption coefficient that made it possible in computing the band gap and other optical parameters studied here in this work.

However there were clearly observed difference especially in the computed band gap as compared to experimentally deduced band gap of the thin film which is bound to be obvious because of some of the assumption that characterized the computation in which lattice dynamics and structures were ignored in the entire formalism. Such deviation also exists in the experimental characterization where the growth techniques, annealing and variation of complexing agents and doping influence the crystallinity of the entire film which invariably results variation in the properties of the thin films. The spectral reflectance of the thin film in this work manifested the same characteristic as showcased in the report of Umeri and Emumejaye, 2015 [3]. This appears as confirmation of the negative characteristic nature of the wave profile within the widow.

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