



Appendix

Multiple Regression Method Solution of the Cumulative-Rate-Time Linear Form

$$\Delta N_p = m_q q + m_{qt} qt + Q_{abs}. \quad (1)$$

Applying multiple regression analysis on linear form in equation (1) above, the forms in equations (2) to (4) below were obtained

$$\sum \Delta N_p = m_q \sum q + m_{qt} \sum qt + n Q_{abs} \quad (2)$$

$$\sum qt \Delta N_p = m_q \sum q^2 t + m_{qt} \sum q^2 t^2 + Q_{abs} \sum qt \quad (3)$$

$$\sum q \Delta N_p = m_q \sum q^2 + m_{qt} \sum q^2 t + Q_{abs} \sum q \quad (4)$$

Solving equations (2) – (4) simultaneously gives,

$$Q_{abs} = \frac{\sum \Delta N_p - m_q \sum q - m_{qt} \sum qt}{n} \quad (5)$$

$$m_{qt} = \frac{(n \sum qt \Delta N_p - \sum qt \sum \Delta N_p) - m_q (n \sum q^2 t - \sum q \sum qt)}{(n \sum q^2 t^2 - (\sum qt)^2)} \quad (6)$$

$$m_q = \frac{(n \sum qt \Delta N_p - \sum qt \sum \Delta N_p) [(n \sum q^2 t - \sum q \sum qt) - (n \sum q^2 t^2 - (\sum qt)^2)] - (n \sum q \Delta N_p - \sum q \sum \Delta N_p) (n \sum q^2 t - \sum q \sum qt)}{(n \sum q^2 t - \sum q \sum qt)^2 - (n \sum q^2 t^2 - (\sum qt)^2) [(n \sum q^2 - (\sum q)^2)]} \quad (7)$$

FLOW CHART FOR MOST ACCURATE FIT OF HYPERBOLIC DECLINE CURVE USING THE CUM-RATE-TIME LINEAR FORM

