Both the Phase Modulation and Frequency Shift Evaluation on Laser Vibrometer

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Abstract

Sinusoidal phase-modulated signal light through the interferometer can produce a beat signal. Moreover, its amplitude monotonically changes with the signal light frequency. So the beat signal amplitude can be used to measure laser-Doppler frequency shift. In addition to the beat signal, the phase-modulated signal also contains a direct current signal, and it still contains a large amount of frequency shift information, but the information is not utilized, resulting in the waste of information. In this paper, this kind of phase-modulated laser-Doppler frequency shift measurement method is improved to simultaneously utilize the useful information in the DC and beat signal for the frequency shift measurement. The specific method is to use the ratio of beat signal amplitude to DC signal amplitude to define a new parameter used in frequency shift measurement. The signal light intensity terms in DC and beat signal can be eliminated, so the improved measurement method does not need to measurement the signal light intensity, which makes its structure further simplified. By comparing the frequency change curves between the newly defined parameter and the beat signal amplitude theoretically, we find that they have the same distribution rule. In theory, by comparing the measurement sensitivity curves, it is proved that the improved phase-modulated frequency shift measurement method has higher measurement sensitivity and dynamic range than the un-improved one.

Keywords: Vibrometer; Frequency; Sensitivity; Phase modulation

Introduction

Laser-Doppler frequency shift measurement method can be used to acquire information (e.g. vibration and speed) of the target. The phase-modulated frequency-shift measurement method has low requirements on light source and optical system and thereby it is easy to be realized. Extracting amplitude (or phase) of phase-modulated beat signal based on coherent detection method can reduce the working bandwidth of the system effectively, thus decreasing the noise power and bringing extremely high measurement accuracy. Nevertheless, The
DC component of phase-modulated signal also contains abundant useful information, but they are not used effectively, resulting in the information waste.

In this paper, this kind of phase-modulated Doppler-frequency-shift measurement method is improved to simultaneously utilize the useful information in the DC and beat signal for the frequency shift measurement, by using the FM signal stimulation, the measurements of phase shift are gotten. The method in this paper can be used to evaluating the frequency shift on laser vibrometer.

**The Phase-Modulated Frequency Shift Measurement Method**

**Principle of Phase Modulation**

The simple-frequency signal after sine phase modulation can be expressed as:

\[ E_{in} = E_0 \exp\left[i(\omega t + \beta \sin \Omega t)\right] \quad (1) \]

Where \( E_0 \) and \( \omega \) are the field intensity and angular frequency of the signal light. \( \Omega \) and \( \beta \) are the sine-phase-modulated angular frequency and modulation index.

Let the modulation signal light run through the interferometer and the photoelectric detector was used for measurement. The output electric signal can be expressed as:

\[ i = i_d + i_{\Omega} + i_{2\Omega} \quad (2) \]

Where \( i_d \) is the DC signal. \( i_{\Omega} \) is the beat signal of the once modulation frequency (generated by the carrier wave and two first-order sidebands). \( i_{2\Omega} \) is the beat signal of the double modulation frequency \( 2\Omega \) (generated by the positive and negative first-order sidebands. It was overlooked in this paper because it is weak).

The period of sine phase modulation was defined \( T_0 = 1/\Omega \), it can be seen from the Equation (2) that at the integral time \( T = nT_0 (n=1,2,3,\ldots) \) of the out signal \( i(t) \) of the detector, the integral results of AC components \( i_d(t) \) and \( i_{2\Omega}(t) \) are zero. In this way, the DC component \( i_d \) can be extracted:

\[ i_d(w) = \frac{1}{T} \int_{0}^{T} i(t)dt \propto E_0^2 h'(w) \quad (3) \]

Since the sine-phase modulation frequency \( \Omega \) is known, it is easy to generate two orthogonal reference signals with the same frequency of beat signal \( i_0(t) \):

\[ \begin{align*}
    i_x(t) &= \sin(\Omega t) \\
    i_c(t) &= \cos(\Omega t)
\end{align*} \quad (4) \]

Through the correlation operation between two reference signals in the Equation (4) and \( i(t) \), it can be get:

\[ R_{srs(c)}(\tau) = \frac{1}{T} \int_{0}^{T} i(t) \cdot i_{srs(c)}(t - \tau) dt \quad (5) \]

The correlation operation of three components of \( i(t) \), namely, \( i_d \), \( i_{\Omega} \), and \( i_{2\Omega} \) was implemented. When the integral time is \( T = nT_0 (n=1,2,3,\ldots) \), the integral results of \( i_d \) and \( i_{2\Omega} \) are zero. Then, the equation (5) can be rewritten as:

\[ \begin{align*}
    R_{srs}(\tau) &= \frac{E_0^2}{2} |A_0| \cos(\Omega \tau - \phi_0) \\
    R_{src}(\tau) &= \frac{E_0^2}{2} |A_0| \sin(\Omega \tau - \phi_0)
\end{align*} \quad (6) \]

It can be seen from the Equation (6) that:

\[ E_0^2 |A_0| \propto 2 \sqrt{\left[R_{srs}(\tau)\right]^2 + \left[R_{src}(\tau)\right]^2} \quad (7) \]

\[ \phi_0 = -\arctan\left[R_{src}(0)/R_{srs}(0)\right] \quad (8) \]

The DC signal \( E_0^2 h' \) and the amplitude \( E_0^2 |A_0| \) and phase \( \phi_0 \) of the beat signal of once modulation frequency can be gained from the above signal processing method. Meanwhile, the light intensity \( E_0^2 \) of signal light can be measured, thus enabling to realize Doppler-frequency-shift.

**Improvement Method**

To use useful information in \( i_d \) and \( i_{\Omega} \) simultaneously, a new frequency demodulation parameter was defined. Its absolute value \( |A_n(w)| \) can use \( R_{srs}(\tau) \), \( R_{src}(\tau) \) and \( i_d \) to get:
It can be seen from the Equation (8) that in the definition process of $|A_n(w)|$, the signal light intensity $E_{n}^{2}$ in $i_d$ and $i_b$ is cancelled simultaneously. This implies that the frequency-shift measurement based on $A_n(w)$ can solve above mentioned problems by indirect use of $E_{0}^{2}$ of $i_d$ only, but doesn’t need to measure $E_{0}^{2}$ directly. Moreover, since $A_n(w)$ is the function of $A_0(w)$ and $h'(w)$, it is used in the measurement, this means that the frequency-shift information in $i_d$ and $i_b$ of the phase-modulated signal are used simultaneously.

**Simulations**

For the comparison, different shapes of shift variation curves of $A_n$ and $A_0$ are shown in Figure 1a. It can be seen from Figure 1b that there’s one upper peak and one low peak on the curve of $A_n(w)$ and the monotonic changes of the curve between these two peaks run through the origin. The overall shape of this section is same with that of the curve of $A_n(w)$. This reveals that frequency-shift measurement based on the curve of $A_n(w)$ is feasible just like the original phase modulation method based on the curve of $A_0(w)$, including using the origin as the working point.

![Figure 1: Curves of $A_n$ and $A_0$ and their absolute sensitivities $\theta_{A_n}$ and $\theta_{A_0}$ changing with frequency.](image_url)

There are some important differences between the curves of $A_n(w)$ and $A_0(w)$. The peak-peak width $L_n$ of the curve of $A_n(w)$ is larger than the peak-peak width $L_0$ of the curves of $A_0(w)$ and the curve of $A_n(w)$ slope is larger than that of the curve of $A_0(w)$. These determine the larger dynamic range and higher sensitivity of frequency-shift measurement based on the curve of $A_n(w)$ compared with those based on the curve of $A_0(w)$.

For the quantitative comparison on dynamic ranges and sensitivity of frequency-shift measurement based on the curves of $A_n(w)$ and $A_0(w)$, the variation curves of their absolute sensitivities $\theta_{A_n(w)}$ are shown in Figure 1b, where $\theta_{A_n(w)} = \left| \frac{dA_n(w)}{dw} \right|$. Both the $\theta_{A_n(w)}$ and $\theta_{A_0(w)}$ curves reach the peak at the working point (origin) and then decrease to zero gradually with the further increase of shift. The frequency-shift position of $\theta_{A_n} = \theta_{A_0} = 0$ in Fig 1b is corresponding to the shift position of peaks of the curves of $A_n(w)$ and $A_0(w)$ in Figure 1 (a), which determines the dynamic range of frequency-shift measurement. The shift range...
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By making the output light frequency change at the step length of 3MHz in the range of $w_0$−150MHz~$w_0$+150MHz. After every change of emergent light frequency, the data acquisition card collect signals output by the photoelectric prober at the sampling frequency of 500MHz, subsequently, sampling data of the photoelectric prober were calculated, getting the values of DC signal $E_0' h'$ and the amplitude $E_0^2 |A_0|$, phase $\phi_0$ of the beat signal. Finally, the measured values of $A_0$ and $A_n$ under different frequency can be gained by the data above and the Equation (6)~(9).

$\frac{L_1}{2} - \frac{L_{n_1}}{2}$ of the curve of $A_n(w)$ is larger than the range $\frac{L_0}{2} - \frac{L_{n_0}}{2}$ of curve of $A_0(w)$, and in this shift range, $\theta_{A_n} > \theta_{A_0}$.

The phase-modulated frequency-shift measurement method was improved by defining a new frequency demodulation parameter. It not only can retain the original working mode of phase modulation, but also doesn’t need to measure the signal light intensity, thus simplifying the system structure and reduce the noise channel. Furthermore it can increase the dynamic range and sensitivity of measurement.

**Experiment and Result**

The experimental apparatus of improved phase-modulated frequency measurement method is shown in Figure 2.
A_\theta and A_\theta at each frequency-shift position were measured by many times and the corresponding average values were calculated. It can be seen by comparing Figure 1a and Figure 3a that the measured curves of A_\theta(w) and A_\theta(w) are very similar with the theoretically calculated curves which prove the accuracy of theoretical analysis.

Partial differential operation of the measured curves of A_\theta(w) and A_\theta(w) in Figure 3a was carried out by numerical calculation, through which the absolute sensitivity ( \theta_\theta and \theta_\theta ) curves of shift measurement were gained Figure 3b. The dynamic range (about -54~62MHz) for shift measurement of A_\theta is larger than that of A_\theta (about -36~43MHz). In the whole dynamic range, there’s \theta_\theta > \theta_\theta , this agrees with the distribution law of theoretical curves in Figure 1(b). It can be seen from distributions of curves ( \sigma_\theta and \sigma_\theta ) that \sigma_\theta and \sigma_\theta are basically same in a small frequency shift range of -25~25MHz, but \sigma_\theta is smaller in the range of about -48~20MHz and 25~52MHz. This proves that A_\theta contributes higher accuracy in frequency shift measurement compared with A_\theta.

Conclusions

DC component of phase-modulation signal includes light intensity information and frequency shift information. However, these information are not used well in previous phase-modulation frequency shift measurement method, resulting in waste of effective information. In this paper, the original phase-modulation frequency shift method is improved to use the useful information in DC component of phase-modulation signals reasonably. The improved method requires no light intensity detector. It not only has simplified structure, but also reduces nose entrance into channels. Experimental results proved the accuracy of the theory, and by using the improved method, the dynamic measurement range and measurement accuracy are all increased.

References
