



Studying Some of Physical Properties of a Lead Doping Titanium Dioxide TiO_2 : Pb with Different Ratios

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Abstract

Titanium dioxide TiO_2 has witnessed great interest in international research laboratories due to its excellent properties. To study the changes in its physical properties, the structural properties of pure and lead-doped titanium dioxide powder samples were examined with different ratios ($x = 0.2 - 0.5 - 0.7 - 0.9$ g).

The results of X-ray diffraction showed the participation of samples of anatase and rutile of the tetragonal crystal system and brookite of the orthorhombic crystal system based in the titanium dioxide compound with the peaks corresponding to the crystalline levels (110), (012), (040), (111), (211), (123), (112). The preferred orientation is (110) in all pure and doped samples. The relative intensities, distance between crystalline planes (d), crystal size (D), lattice parameters (a), (b) and (c), Initial cell size (V), dislocation density (δ), and theoretical density of the X-ray diffraction spectrum for the powders ($\rho_{\text{X-ray}}$) were determined, and the number of atoms of a substance per unit volume (n) and the average distance between atoms (L).

Keywords: Powder; Titanium dioxide TiO_2 doped with lead Pb; Structural properties; Physical properties; XRD

Introduction

Titanium dioxide TiO_2 has gained great attention, especially under the conditions of the COVID-19 pandemic. After the sun's rays fall on this material, active oxygen is generated, which in turn purifies water from pollutants, bacteria, fungi, germs, organic materials, as well as toxic elements such as arsenic As and Chromium Cr [1-3]. Titanium was first discovered in 1971 by an English chemist and geologist William Gregor and years later, titanium dioxide TiO_2 was manufactured for use as a whitening ingredient used in toothpastes, a multifaceted compound used as a strong photocatalyst capable of breaking any organic compound if exposed to the sun [4-15], and therefore can be

used in cleaning and bleaching fabrics and purifying water / waste water and air [16] and in many other industrial applications such as the iron, electronics and chemicals industry, all the way to the manufacture of cosmetics, batteries and solar cells [17] and hydrogen production because of its important physical and chemical properties. It has chemical stability and is chemically non-toxic [2,3] and a high static permittivity, and is characterized by an Eg energy gap ranging between 3.04-3.46 eV [18], as it has a high resistivity estimated at $10^{12} \Omega \cdot \text{cm}$ at a temperature of 25°C. It also has high transparency in the visible field, high refractive index, and high luminescence, which expands its uses as a paint in all types of paint and as a food additive for pharmaceutical materials [7,19]. Titanium dioxide TiO_2

also has structural properties, as it is found under different crystalline phases: Anatase with a tetragonal crystal system,

brookite with a orthorhombic crystal system, and rutile with a tetragonal crystal system as in Figure 1 [20].

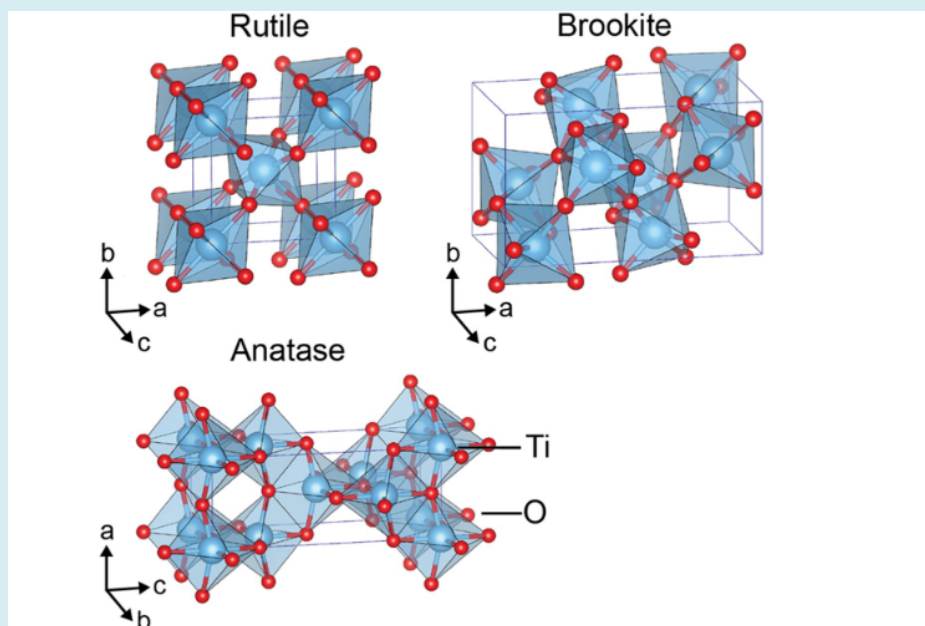


Figure 1: Crystal structure of TiO_2 rutile (tetragonal, $P4_2/mmm$), brookite (orthorhombic, $Pbca$) and anatase (tetragonal, $I4_1/amd$) polymorphs.

All of these properties have expanded its uses in the modern era to include gas detectors such as H_2 , O_2 , CO and $\text{C}_2\text{H}_5\text{OH}$ [21] and in medicine such as artificial heart valve and semiconductors and storing capacitors in dynamic random memories and in integrated circuits and assistants. We chose the Pb element as an impurity in the compound TiO_2 and it is an element known since ancient times. Statues and tools made of it were found in the tombs of the ancient Egyptians, as were found in antiquities dating back to the Aegean civilization 1400-1100 BC [22] in southern Greece Figure 2 shows some of its physical properties that distinguish it from the rest of the elements.

In this research, we prepared samples of leaded titanium dioxide in different proportions, $\text{Pb}:\text{TiO}_2$, and then we crushed these samples separately, sieved them and calcined them from 0°C to 200°C to remove moisture and used X-ray diffraction device (XRD) in order to study the properties The structural properties of these samples in order to improve the physical properties and expand the effectiveness and areas of use of titanium dioxide after many researchers have doped it with different chemical elements and compounds using each of the XRD, SEM, DRS, EDS, FT-IR devices and others, which showed the displacement of the radiation absorption field from ultraviolet rays to include raising the efficiency of absorption of these rays as well as light rays, narrowing the

band gap, and thus increasing the photocatalytic property [23], electrical conductance and other electronic, physical and microscopic properties [2,4,7,10,12-15,18,19,24-26].

Experimental Method

We weighed powders of pure and lead doped TiO_2 with different ratios according to ($x = 0.2 - 0.5 - 0.7 - 0.9 \text{ g}$) $\text{Ti}_{1-x}\text{Pb}_x\text{O}_2$ using solid-state interaction method [27] and [28], and it was mixed and crushed well using (Agate mortar and pestle) to turn it into powders very fine and then sieved through a sieve giving the size of the opening of the sieve 90 microns. The mixtures were ground for two hours for all powder samples in order to obtain a homogeneous and well-distributed powder. To remove moisture, the crushed samples were heated to 200°C by an incinerator, as all the preparation process took place in the physics and chemistry laboratories at the Faculty of Science at Tishreen University.

Results and Discussion

X-ray Diffraction Test

The XRD pattern show the participation of all the undoped and Pb doped TiO_2 powders with the peaks corresponding to the crystalline levels (110), (012), (040),

(111), (211), (123), (112), (220). Preferred orientation is (110) in all undoped and Pb doped samples, while the peaks corresponding to levels (210), (213), (160), (203) disappear or shift in The similar sample whose percentage of lead equals 0.9 g, while the corresponding peak of the level (220)

disappears or shifts in the similar sample whose percentage of lead equals 0.7 g. It was also noted with different doping ratios that there is an absence of some peaks corresponding to pure titanium dioxide and the appearance of new peaks due to lead impurity (Figure 2).

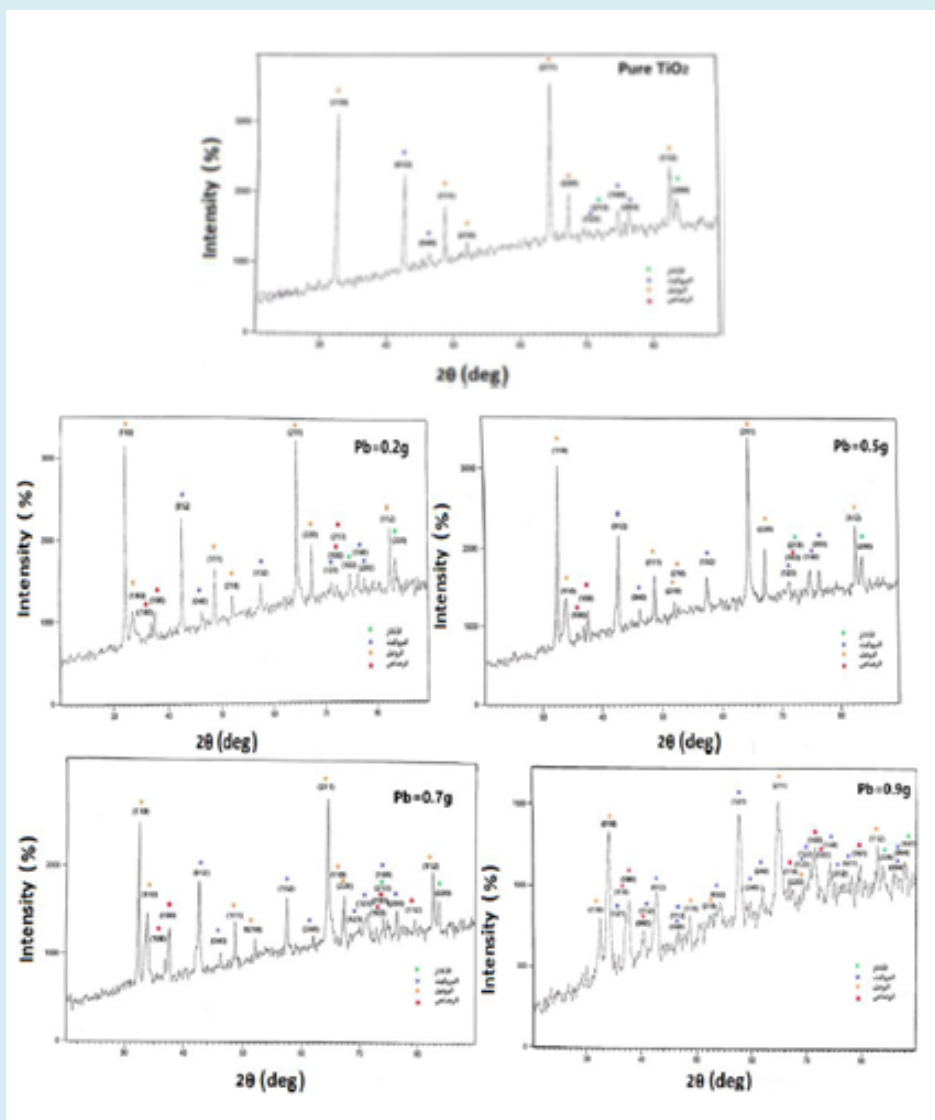


Figure 2: XRD results of pure and lead-doped TiO_2 samples ($x = 0.2 - 0.5 - 0.7 - 0.9$ g).

We calculated the relative intensity of the pure and lead-dominated TiO_2 powders. The distance values between crystal planes were calculated using the following Bragg's law [29]:

$$2d \sin \theta = n\lambda \quad (1)$$

Where d is the distance between crystal planes in angstroms (Å) and θ is Bragg's angle in radians (rad) and λ is the wavelength of the x-rays ($\lambda = 1.78897 \text{ Å}$) and we calculated

the crystallite size from Scherrer's equation [30]:

$$D = \frac{k\lambda}{\beta \cos \theta} \quad (2)$$

where D is the crystal size in nanometer (nm).

K is Scherrer's constant, so for a cubic crystal system it takes the value 0.94, and for a non-cubic crystal system it takes the value 0.89 and therefore the value we use is the last value [31].

λ is the wavelength of x-rays measured in angstrom (\AA).
 β is the full width at half maximum intensity (FWHM) measured in radians.
 θ is the Bragg's angle, also measured in radians.

The dislocation density δ is defined as the length of the dislocation lines per unit volume and is calculated from the following equation [32]:

$$\delta = \frac{1}{D^2} \quad (3)$$

The lattice constants a (\AA), b (\AA) and c (\AA) for the tetragonal crystal system of the anatase, rutile and orthorhombic crystal system of the brookite phase were determined from the equations (4) and (5), respectively [18] & [33]:

$$\frac{1}{d^2} = \frac{h^2}{a^2} + \frac{k^2}{b^2} + \frac{l^2}{c^2} \quad (5)$$

where $a = b \neq c$; for anatase and rutile phases just.

where d is the distance between two successive one

angstroms of crystal planes in angstroms (\AA) and (hkl) are the Miller indices. The grid constants a (\AA), b (\AA) and c (\AA) given in Tables 1, 2, 3 were also calculated, which match well with the JCPDS data. were also calculated, for brookite, ($a = 5.455 \text{\AA}$, $b = 9.18 \text{\AA}$, $c = 142 \text{\AA}$), and for rutile ($a = b = 4.593 \text{\AA}$, $c = 2.959 \text{\AA}$), and for anatase ($a = b = 3.785 \text{\AA}$, $c = 9.513 \text{\AA}$), and for lead Pb ($a = b = 3.265 \text{\AA}$, $c = 5.387 \text{\AA}$). The change in peak intensity is mainly due to the replacement of Ti^{4+} ions by Pb^{4+} ions in the TiO_2 lattice. We also computed initial cell size from relation [34]:

$$V = a \cdot b \cdot c \quad (6)$$

where a , b , c are the crystal lattice constants given in Tables 2-6.

This process leads to the movement of Pb^{4+} ions into the substitution sites. It was observed that the increase in the doping ratio increases the size of the primary cell, the size of the crystal, the relative intensity, and the density of the dislocation decreases, and this is consistent with the researchers [26] and [35]. We observed from Tables 2, 3 & 4 that 0.2g lead-doped TiO_2 is the closest value to the undoped sample.

Sample	2θ (deg)	(hkl)	d (\AA)	Rel. Int. (%)	β (deg)	D (nm)	\bar{D} (nm)	$\delta \cdot 10^{15}$ Line/m ²	Lattice Constants for Phases			Phases Cell Size $V(\text{\AA})^3$
									a (\AA)	b (\AA)	c (\AA)	
Pure TiO_2	32.1	(110)	3.236	100	0.4	23.732		1.776				
	42.355	(012)	2.477	25	0.355	27.559	118.236 for anatase	1.317				
	46	(040)	2.29	5	0.3	33.035		0.917	3.794	3.794	9.408	135.352 for anatase
	48.5	(111)	2.178	25	0.4	25.014		1.599				
	51.8	(210)	2.048	10	0.2	50.706	40.303 Lilbrooke	0.389				
	64.4	(211)	1.679	60	0.25	43.123		0.538	5.539	9.16	5.139	260.74 Lilbrooke
	67	(220)	1.621	20	0.4	27.35		1.337				
	71	(123)	1.541	7	0.25	44.822	35.08 Lalrutel	0.498				
	73.7	(213)	1.492	4	0.1	114.003		0.077				
	74.9	(160)	1.472	4	0.2	57.456		0.303	4.577	4.577	2.946	61.72 Lalrutel
	76.2	(203)	1.45	12	0.3	38.642	64.54 For Phases Together	0.67				
	83	(112)	1.35	12	0.3	40.602		0.607				
83.7	(220)	1.341	60	0.1	122.468	0.067						

Table 1: The results of the structural values of pure TiO_2 sample.

Sample	2θ (deg)	(hkl)	d(A°)	Rel. Int. (%)	β (deg)	D (nm)	\bar{D} (nm)	$\delta \cdot 10^{15}$ Line/m ²	Lattice Constants for Phases			Phases Cell Size V(A°) ³
									a(A°)	b(A°)	c(A°)	
Lead-doped TiO ₂ (x=0.2g)	32.1	(100)	3.236	100	0.425	22.355		2.002				
	33.6	(110)	3.095	100	0.03	317.642		0.01				
	36.7	(100)	2.842	75	0.1	96.113		0.109				
	37.4	(100)	2.79	75	0.2	48.155	82.696	0.432	3.793	3.793	9.408	135.352
	42.36	(012)	2.477	25	0.3	32.612	Anatase	0.941				
	46	(040)	2.29	5	0.18	55.058		0.33				
	48.5	(111)	2.178	25	0.5	20.011		2.498				
	51.8	(210)	2.048	10	0.1	101.412	47.849	0.098				
	57.7	(210)	1.854	10	0.2	52.077	Brookite	0.369				
	64.4	(211)	1.679	60	0.3	35.936		0.775				
	67	(220)	1.621	20	0.24	45.583		0.482	5.539	9.16	5.146	261.094 Brookite
	71	(123)	1.541	7	0.18	62.253		0.259				
	71.9	(512)	1.524	5	0.24	46.954	83.105	0.454				
	72.4	(103)	1.515	20	0.12	94.207	Rutile	0.113				
	73.7	(013)	1.492	4	0.18	63.335		0.25	4.577	4.577	2.945	61.695 Rutile
	74.9	(160)	1.472	4	0.18	63.839		0.246				
	76.2	(203)	1.45	12	0.22	52.694		0.361				
	83	(112)	1.35	12	0.28	43.502		0.529				
83.7	(220)	1.341	6	0.12	102.057		0.961					

Table 2: Results of the structural values of the lead-doped TiO₂ sample (x = 0.2 g).

Sample	2θ (deg)	(hkl)	d(A°)	Rel. Int. (%)	β (deg)	D (nm)	\bar{D} (nm)	$\delta \cdot 10^{15}$ Line/m ²	Lattice Constants for Phases			Phases Cell Size V(A°) ³
									a (A°)	b (A°)	c (A°)	
Lead - Doped TiO ₂ (x=0.5g)	32.1	(110)	3.236	100	0.3	31.642		0.999				
	33.6	(110)	3.095	100	0.3	31.765		0.992	3.793	3.793	9.408	135.352 Anatase
	36.7	(100)	2.842	75	0.05	192.226	88.324 Anatase	0.028				
	37.4	(100)	2.79	75	0.2	48.155		0.432				
	42.355	(012)	2.477	25	0.2	48.917		0.418				
	46	(040)	2.29	5	0.2	49.552		0.408				
	48.5	(111)	2.178	25	0.3	33.352	99.547 Brookite	0.899	5.539	9.16	5.146	261.094 Brookite
	51.8	(210)	2.048	10	0.1	101.412		0.098				
	52.3	(411)	2.03	7	0.1	101.628		0.097				
	57.7	(132)	1.854	18	0.4	26.039		1.475				
	64.4	(211)	1.679	60	0.2	53.904		0.345				
	67	(220)	1.621	20	0.1	109.398	48.382 Rutile	0.084				
	71	(103)	1.541	20	0.15	74.704		0.18				
	72.4	(103)	1.515	20	0.08	141.311		0.051				
	73.7	(213)	1.492	4	0.12	95.002		0.111	4.577	4.577	2.945	61.695 Rutile
	74.9	(160)	1.472	4	0.05	229.821		0.019				
	76.2	(203)	1.45	12	0.2	57.963	78.752 For phases together	0.298				
	83	(112)	1.35	12	0.2	60.559		0.273				
83.7	(220)	1.341	6	0.15	81.646		0.151					

Table 3: Results of the structural values of TiO₂ sample doped with lead (x = 0.5 g).

Sample	2θ (deg)	(hkl)	d(A°)	Rel. Int. (%)	β (deg)	D (nm)	\bar{D} (nm)	$\delta \cdot 10^{15}$ Line/m ²	Lattice Constants for Phases			Phases Cell Size V(A°) ³
									a (A°)	b (A°)	c (A°)	
Lead-doped TiO ₂ (x=0.7g)	32.1	(110)	3.236	100	0.3	31.642		0.999				
	33.6	(110)	3.095	100	0.6	15.883		3.965				
	36.7	(100)	2.842	75	0.3	32.038	89.735 Anatase	0.975				
	37.4	(100)	2.79	75	0.4	24.078		1.725				
	42.355	(012)	2.477	25	0.3	32.611		0.941	3.793	3.793	9.408	135.352 Anatase
	46	(040)	2.29	5	0.4	24.776		1.63				
	48.5	(111)	2.178	25	0.24	41.69	49.802 Brookite	0.576				
	51.8	(210)	2.048	10	0.34	29.827		1.125				
	57.7	(132)	1.854	18	0.2	52.077		0.369				
	62.3	(240)	1.73	3	0.2	53.298		0.353				
	64.4	(211)	1.679	60	0.21	51.337		0.38	5.539	9.16	5.146	261.094 Brookite
	66.4	(110)	1.634	70	0.1	109.022		0.085				
	67	(220)	1.621	20	0.4	27.35		1.337				
	70	(123)	1.59	7	0.1	111.366	32.598 Rutile	0.081				
	71	(123)	1.541	7	0.4	28.014		1.275				
	71.9	(103)	1.524	20	0.12	93.908		0.114				
	72.4	(103)	1.515	20	0.21	53.833		0.346	4.577	4.577	2.945	61.695 Rutile
	73.7	(213)	1.492	4	0.2	57.002		0.308				
	74.9	(160)	1.472	4	0.3	38.304		0.682				
	76.2	(203)	1.45	12	0.2	57.963		0.298				
79.5	(112)	1.399	35	0.2	59.327	57.379 For phases together	0.285					
83	(112)	1.35	12	0.4	30.451		1.079					
83.7	(220)	1.341	6	0.1	122.468		0.067					

Table 4: Results of the structural values of TiO₂ sample doped with lead (x = 0.7 g).

The preferred orientation along the plane (211) for all samples, as the reason for the peak corresponding to the previous plane is due to the presence of crystals from the rutile phase, regardless of the percentage of doping.

And we note that brookite crystallizes in the direction (012) for all the pure and lead-doped samples. As for the lead - doped sample by x=0.9g, it crystallizes in the direction (121) and anatase crystallizes in the direction (200) for all samples except the lead - doped sample by x = 0.9g as it crystallizes according to the direction (220) and lead crystallizes according to the direction (100) for all samples except for the sample with a doping ratio of x = 0.9g, it crystallizes according to the direction (110) and the

reason is that those samples maintained their direction up to the dopance ratio x = 0.9g is that at that ratio there was the largest increase in crystal size and the largest increase in cell size, and this explains that this alloy is likely to cancel some of the grain boundary when the grains coalesce to form crystals of larger size, as well as canceling the defects that exist after the occurrence of The process of natural growth of crystals and rearrangement of crystal grains , as the grains take enough energy for the natural growth of crystals and arrangement within that lattice, as these limits were impeding the movement of electrons and canceling some of them, the electrical conductivity in the metallic material increases due to diminished for electrical resistance [25].

Sample	2θ (deg)	(hkl)	d(A°)	Rel. Int. (%)	β (deg)	D (nm)	\bar{D} (nm)	$\delta \cdot 10^{15}$ Line/ m ²	Lattice Constants for Phases			Phases Cell Size V(A°) ³
									a (A°)	b (A°)	c (A°)	
Lead-doped TiO ₂ (x=0.9g)	32.1	(110)	3.236	100	0.5	18.986		2.775				
	33.6	(110)	3.095	100	0.6	15.883		3.965				
	35.7	(121)	2.919	90	0.2	47.92		0.436				
	36.7	-100	2.842	75	0.15	64.076		0.244				
	37.4	(100)	2.79	75	0.1	96.31		0.108				
	39.6	(002)	2.641	30	0.2	48.479		0.426	3.793	3.793	9.502	136.704 Anatase
	42.355	(012)	2.477	25	0.2	48.917	62.565 Anatase	0.418				
	46	(040)	2.29	5	0.2	49.552		0.408				
	46.5	(112)	2.266	8	0.1	99.289		0.102				
	48.5	(111)	2.178	25	0.26	38.483		0.676				
	52.3	(210)	2.03	10	0.04	254.07		0.016				
	53.5	(032)	1.988	16	0.2	51.08		0.384				
	54.5	(102)	1.954	10	0.21	48.864		0.419				
	57.7	(102)	1.854	10	0.2	52.077		0.369				
	61.215	(240)	1.757	3	0.11	96.358		0.108				
	61.25	(332)	1.756	26	0.08	132.515		0.057				
	64.4	(240)	1.679	3	0.1	107.807	94.31 Brookite	0.087	5.539	9.16	5.146	263.428 Brookite
	66.4	(110)	1.634	70	0.2	54.511		0.337				
	67	(220)	1.621	20	0.05	218.796		0.021				
	70	(440)	1.56	5	0.08	139.208		0.052				
	71	(123)	1.541	7	0.2	56.028		0.319				
	71.9	(512)	1.524	5	0.1	112.69		0.079				
	72.4	(103)	1.515	20	0.1	113.049	99.233 Rutile	0.079				
	74.9	(160)	1.472	4	0.2	57.456		0.3030				
	75	(600)	1.47	2	0.2	57.494		0.3026	4.577	4.577	2.945	61.695 Rutile
	78.4	(611)	1.416	9	0.08	147.149		0.047				
	79.5	(112)	1.399	35	0.2	59.327		0.285				
	83	(112)	1.35	12	0.3	40.602		0.607				
83.7	(220)	1.341	6	0.2	61.234		0.267					
87.6	(00)4	1.293	2	0.1	126.393	85.37 For phases together	0.063					
87.8	(004)	1.29	2	0.05	253.211		0.016					
88.9	(107)	1.278	<2	0.2	63.896		0.245					

Table 5: Results of the structural values of TiO₂ sample doped with lead (x = 0.9 g).

We also note that with the increase in the ratios of doping, new peaks appeared for the three phases and for lead, and most of the peaks were for the brookite phase among the three phases, which increased with the increase in the ratios of doping. (2θ) with an increase in the doping ratio and the

explanation for this displacement is due to the small ionic radius of titanium (0.745 A°) compared to the ionic radius of lead impurity (11.950 A°). An ionic diameter greater than 0.8 A° leads to a decrease in the crystal size of TiO₂ due to a decrease in the distance between the crystalline levels (d)

and then an increase in the diffraction angle, and thus the displacement of the characteristic peaks towards the right in the diffraction pattern because it has an inverse relation

according to Bragg's law [29] as stated in Pauling's principle [36-38].

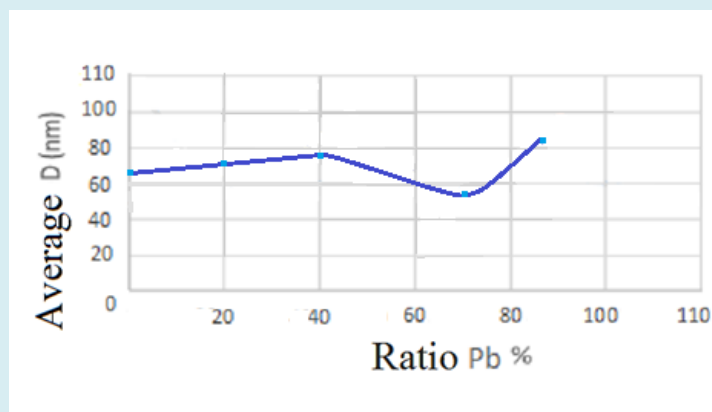
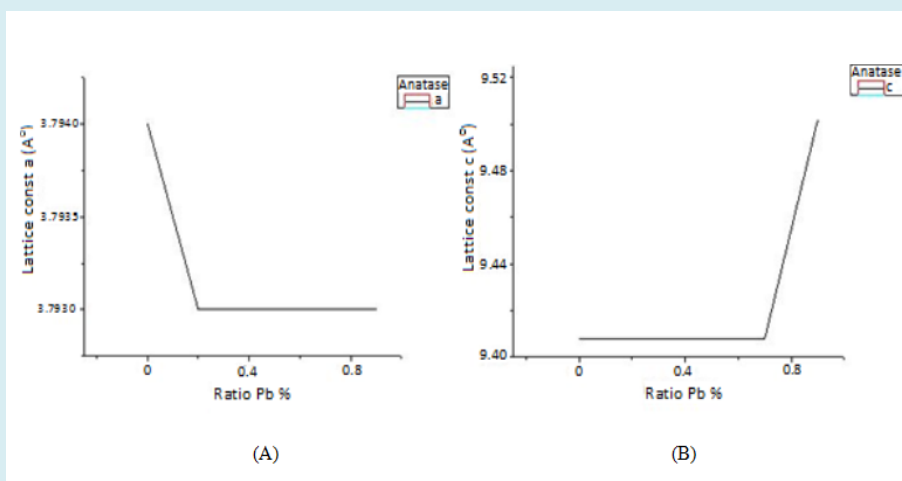


Figure 3: Variation of average particle size in different proportions of lead-doped TiO₂ powders taken together (anatase, brookite, and rutile).

Figure 3 shows that the average crystal size of the 0.2g lead-doped sample is closer to that of the pure sample, However, the decrease in the average crystal size increase of 0.7g compared to the other similar samples and may be due to the linear increase in the average size The crystal starting from the pure compound and passing through each of the doping ratios with 0.5g and 0.2g lead indicates that the impurities effectively prevent the growth of the granules by forming dissimilar boundary regions and because of the increase in the doping ratio that causes the increase in the crystal size and this agrees with the researcher [8] It is known that the increase in the particle sizes reduces the stress in the grain boundaries resulting from the crushing process. These boundaries are suitable locations for the sites of defects and crystal impurities that lead to the enhancement of the electrical resistance and thus the electrical conductivity will

increase [12] and Since the phases have no difference in chemical composition between them, while there is a change in the atomic arrangement and crystal orientation across the phase boundaries, the surfaces that separate them are not similar in energy and composition to the grain boundaries with a small inclination angle, It is possible that the presence of crystal defects in the dopant sample with a percentage of 0.7g is the reason for the change of the linear increase, as we noticed a decrease in the crystal size at it (57.379), where we note in Table 4. The decrease in the size of the grains in both brookite and rutile except for anatase [11]. The crystal size of the three phases together falls within the range [57.379-85.370 nm], distributed over anatase [62.565-118.236 nm], brookite [40.303-94.310 nm] and rutile [35.080-99.233 nm] and this is consistent with the researcher Fouzia A and Bensaha R [26].



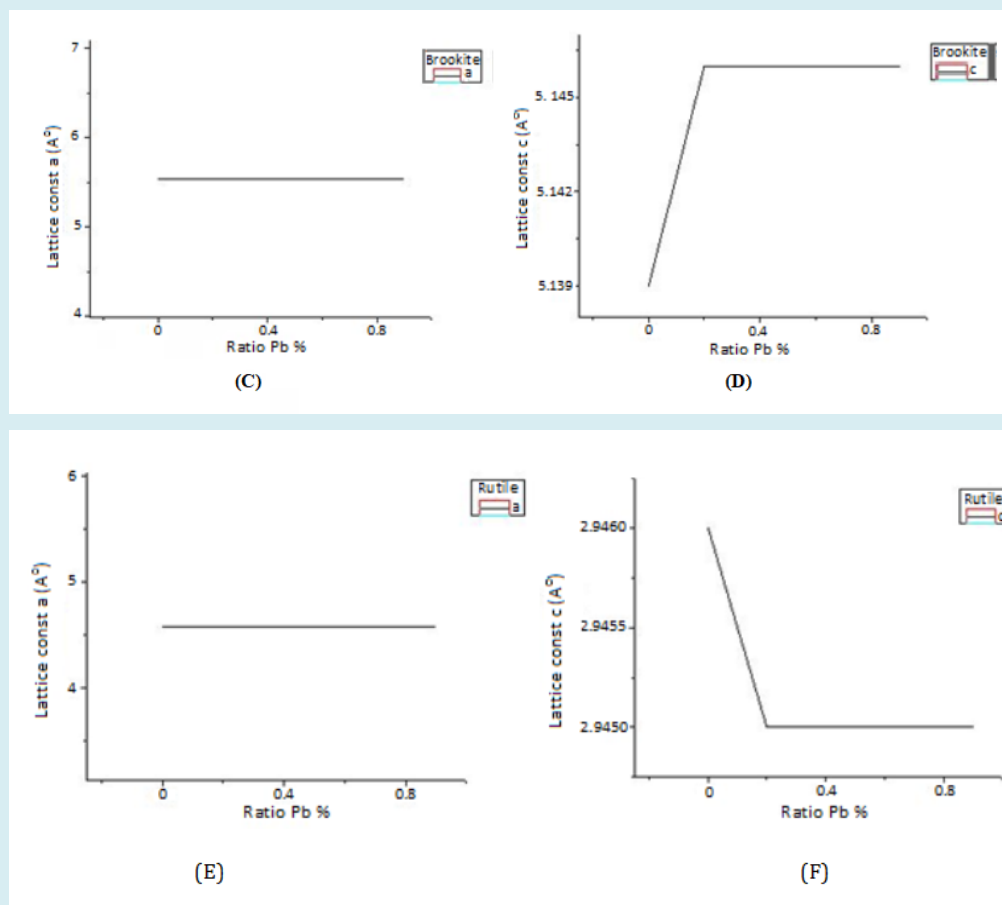


Figure 4: The crystal lattice constants a (Å), c (Å) in the anatase phase (A), (B), respectively, for the compound of pure and lead-doped titanium dioxide in different ratios ($x = 0.2 - 0.5 - 0.7 - 0.9$ g), the brookite (C) and (D) phase, respectively, for the compound of pure and lead - doped titanium dioxide in different ratios ($x = 0.0 - 0.2 - 0.5 - 0.7 - 0.9$ g), the rutile (E) and (F) phase, respectively, for the compound of pure titanium dioxide doped with lead in different proportions ($x = 0.2 - 0.5 - 0.7 - 0.9$ g).

It is possible that the increase in one of the crystal lattice constants a , b or c is due to the increase in vacancies, the stretching of the crystal lattice and the increase in the size of the primary cell and vice versa [39] (Figure 4). The expansion of the z -axis and this expansion in the basal plane is due to an increase in crystal vacancies and vice versa for rutile in which the constant c has decreased. Its decrease in anatase at the first rate of doping while maintaining a constant value until the last percentage of doping due to the contraction of each of the x and y axes and a decrease in the possibility of voids resulting from the occurrence of fault stacking during the process of natural crystal growth of the material according to this level of the crystal structure of the material and the occurrence of shrinkage of the quaternary crystal lattice, and the increase in the lattice constants is due to the increase in the distance between the crystal levels, and this agrees with the researcher Yu J, et al. [5].

Then we calculated the Theoretical density of the X-ray diffraction spectrum for pure and dopant samples using the equation (7) [40] (Table 7):

$$\rho_{X\text{-ray}} = \frac{Z M_{wt}}{N_a V} \quad (7)$$

$\rho_{X\text{-ray}}$: The theoretical density of the X-ray diffraction spectrum for powders is g/cm^3 .

Where Z : The number of atoms per unit cell, which is 2 in the rutile phase, 8 in the brookite phase, and 4 in the anatase phase.

M_{wt} : The molar mass is g/mol , which is 79.866 g/mol for the three phases of TiO_2 .

N_a : Avogadro's number $6.023 \times 10^{23} \text{ mol}^{-1}$.

V : The initial cell size given in Tables (2-6) whose unit is $(\text{Å})^3$.

Samples	Pure TiO ₂	$\rho_{X\text{-ray}}$ (g/cm ³)			
		Lead-doped TiO ₂ (x=0.2g)	Lead-doped TiO ₂ (x=0.5g)	Lead-doped TiO ₂ (x=0.7g)	Lead-doped TiO ₂ (x=0.9g)
Rutile	4.297	4.299	4.299	4.299	4.299
Anatase	3.919	3.919	3.919	3.919	3.881
Brookite	4.069	4.063	4.063	4.063	4.027
All phases	4.096	4.094	4.094	4.094	4.069

Table 7: Theoretical density of pure and lead-doped TiO₂ powders (0.2 - 0.5 - 0.7 - 0.9 g).

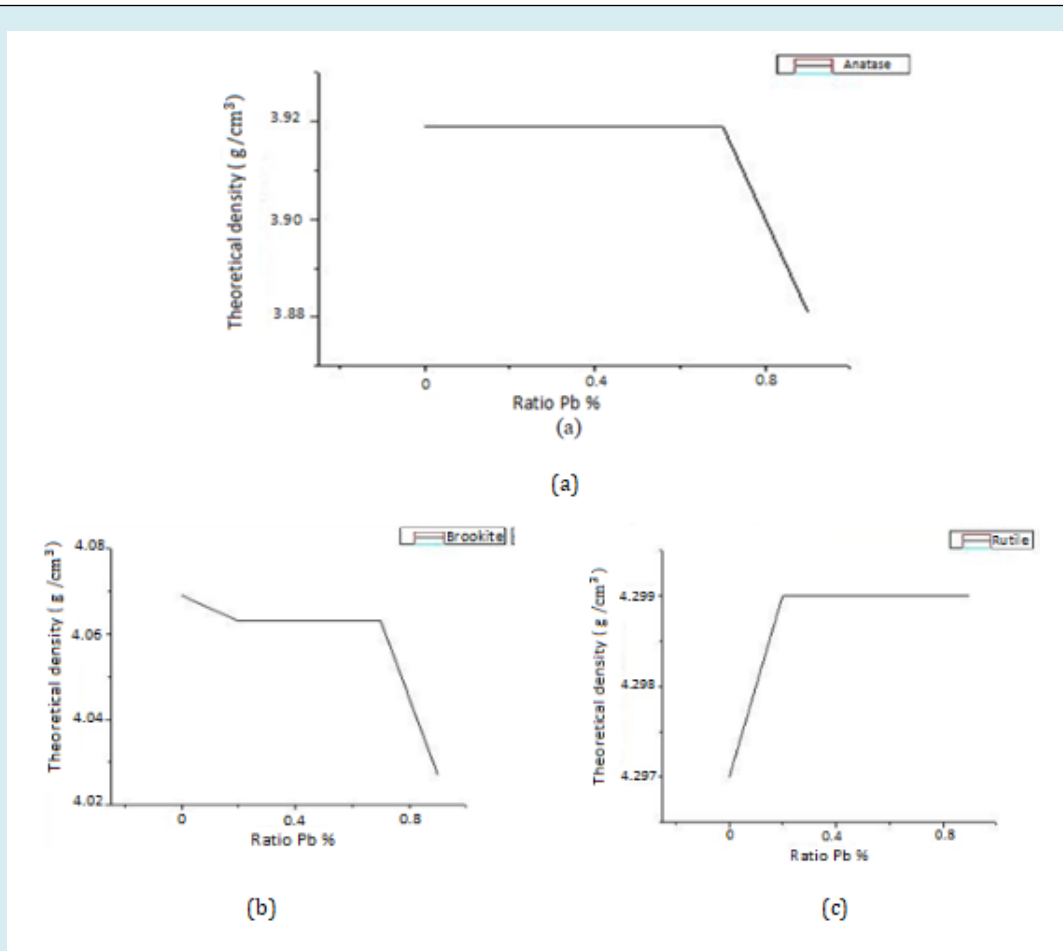


Figure 5: Theoretical density $\tilde{n}_{X\text{-ray}}$ in the phases of anatase (a), brookite (b) and rutile (c), respectively, for samples of pure and lead-doped titanium dioxide in different ratios ($x = 0.2 - 0.5 - 0.7 - 0.9$ g).

We note that the theoretical density $\tilde{n}_{X\text{-ray}}$ decreased with the increase of the dopance due to the increase in the cell size with the increase in the dopance from the inverse relationship between the two parameters [40] (Figure 5), because the cell size decreased by the same value for all ratios compared to pure rutile by increasing the dopant ratio, the lattice coefficients and the theoretical density, which we note that there is no change in it, remain constant until certain dot ratios. The change in the stability of the previous

parameters [25].

The number of material atoms can also be calculated using the relation (8) [41] (Table 8):

$$n = N_a \frac{\rho_{X\text{-ray}}}{M_{wt}} \quad (8)$$

n : the number of atoms of a substance in a unit volume of

atom/cm³.

N_a : Avogadro's number $6.02 \times 10^{23} \text{ mol}^{-1}$.

$\rho_{X\text{-ray}}$: The theoretical density of the X-ray diffraction

spectrum for powders is g/cm³.

M_{wt} : The molar mass is g/mol, which is 79.866 g/mol for the three phases of TiO₂.

n 10 ²² (atom/cm ³)					
Samples	Pure TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂
		(x=0.2g)	(x=0.5g)	(x=0.7g)	(x=0.9g)
Rutile	3.241	4.243	4.243	4.243	4.243
Anatase	2.956	2.956	2.956	2.956	2.927
Brookite	3.069	3.065	3.065	3.065	3.037
All phases	3.089	3.422	3.422	3.422	3.403

Table 8: the number of atoms of pure and lead-doped TiO₂ powders (0.2 - 0.5 - 0.7 - 0.9 g).

We note the increase in the number of substance atoms per unit volume with an increase in the percentage of doping, but this increase slightly decreased at the doping percentage with lead g 0.9, and this is related to the previous changes that occurred in the theoretical density of the X-ray diffraction spectrum for powders due to the direct proportionality between these two parameters.

By calculating n, we can calculate the average distance between atoms in nanometer unit, for materials in which the number of atoms per unit volume is within $n = 6 \times 10^{22} \text{ atom/cm}^3$ by substituting in the equation (9) [14] (Table 9):

$$L = (n)^{1/3} \text{ (9)}$$

L (nm)					
Samples	Pure TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂	Lead-doped TiO ₂
		(x=0.2g)	(x=0.5g)	(x=0.7g)	(x=0.9g)
Rutile	0.319	0.349	0.349	0.349	0.349
Anatase	0.31	0.31	0.31	0.31	0.309
Brookite	0.314	0.313	0.313	0.313	0.312
All phases	0.314	0.325	0.325	0.3247	0.3241

Table 9: The average distance between atoms of of pure and lead-doped TiO₂ powders (0.2 - 0.5 - 0.7 - 0.9 g).

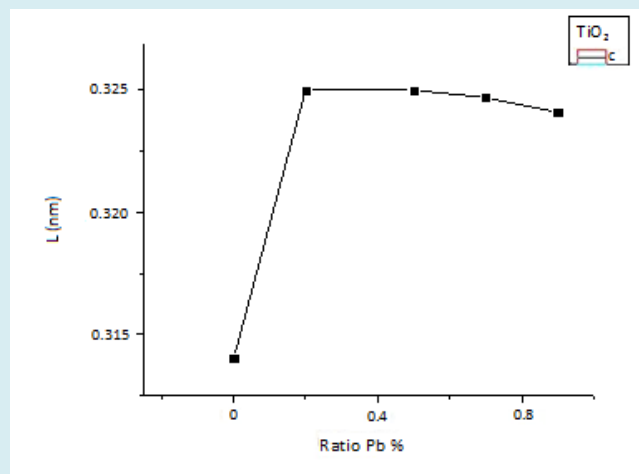


Figure 6: The average distance between atoms L (nm) for samples of pure and lead-doped titanium dioxide in different ratios (x = 0.2 - 0.5 - 0.7 - 0.9 g).

We notice the linear increase in the distance between the atoms in the two samples of pure and lead-doped titanium dioxide with a ratio of 0.2 g, then this increase was fixed at the dopance ratio of 0.5 g, while at the ratio of 0.7 g it took a decrease to reach the dopance ratio of 0.9 g. And with the decreasing distance between the atoms and their approach to the constants of the crystal lattice, the dissolution of the intermittent energy levels occurs and energy bands are formed, the width of which decreases as we go deeper inward towards the nucleus (Figure 6). The permissible energy bands separate, with forbidden bands E_g that cannot be occupied by electrons, and thus the interaction between them increases and the height and width of the voltage barrier between atoms decreases, as the decrease in height leads to the fall of the final atomic level above the voltage barrier, which makes the electron free to That level, as these electrons match perfectly with all atoms of the substance, forming a so-called electronic gas, which facilitates the passage of internal electrons (other than valence electrons) through the barriers that separate neighboring atoms and their movement within the crystal itself and the ability of electrons to meet. In our study, we take into consideration that the atoms are composed of spheres with a net positive charge resulting from the nucleus (Ti^{+4} and Pb^{+4}) in addition to the electrons of the inner core of the atom, since the potential energy is closely related to the distance between the atoms. We note that at 0.9 g of doping of lead, the potential energy and bonding forces between the atoms are the largest compared to the other doping ratios due to the decrease in the distance between the atoms at this ratio of doping. When the atoms get close to each other, the orbitals overlap and the valence electrons begin to rearrange themselves until they reach to a more stable arrangement, and during this rearrangement, different types of bonds are formed between the atoms and this rearrangement causes an increase in the cohesion of the atoms and the formation of the solid state.

Conclusions

This paper presents a study of the structural properties that explain some physical properties of TiO_2 powders doped with lead in different ratios.

XRD Patterns Confirmed. The XRD results showed that samples of anatase and rutile of the quaternary crystal system and brookite of the rhombic crystal system based in titanium dioxide have peaks corresponding to the crystalline levels (110), (012), (040), (111), (211), (123), (112), (220). All samples prefer the direction along the plane (110). The average crystal size (D) of the three phases together is in the range [57.379-85.370 nm]. And by calculating the distance between the crystalline levels (d), the lattice parameters (a), b) and c) and the size of the cell phases (V), the theoretical density of the X-ray diffraction spectrum of the powders $\bar{n}_{X\text{-ray}}$

is within the range [4.69-4.096 g/cm³] And we calculated the number of atoms for each sample per unit volume (n), so the average distance between the atoms (L) for the three phases together within the range [0.3140-0.3250 nm] The lattice constants were a(A°), b (A°), c (A°) for all samples are nearly identical to the JCPDS values.

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